

ECOLE NATIONALE SUPERIEURE DES TRAVAUX PUBLICS (ENSTP)  
YAOUNDE

End of Course Re-sit Examinations 2020/2021

Subject: ELE303 - Fundamentals of Electrical Engineering

Time Allowed: 3 hours

Lecturer: Dr. Engr. MBINKAR Edwin

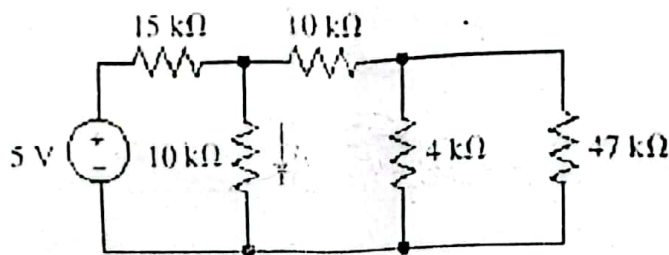
Answer all (4) four questions. You are reminded of the necessity for orderly presentation of your answers. Documents are NOT allowed. Start answering each question on a new page.

Note: All questions carry equal marks

ELE303

**Question 1**

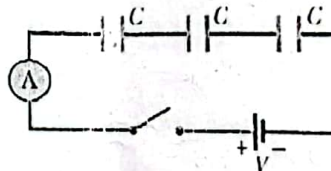
For the circuit below, determine  $i_x$ , and compute the power dissipated by (or absorbed by) the 15-k $\Omega$  resistor.



**Question 2**

(a) The figure below shows an open switch, a battery of potential difference  $V$ , a current-measuring meter  $A$ , and three identical uncharged capacitors of capacitance  $C$ . When the switch is closed and the circuit reaches equilibrium, what are:

- the potential difference across each capacitor and
  - the charge on the left-hand plate of each capacitor?
- Give your answers in terms of  $C$  and  $V$ .



- (b) Most homes use solid copper wire having a diameter of 1.63 mm to provide electrical distribution to outlets and light sockets. Determine the resistance of 75 meters of a solid copper wire having the above diameter. Take the resistivity of copper to be  $1.723 \times 10^{-8} \Omega\text{m}$ .

**Question 3**

Draw the schematic diagram of a single-phase, full-wave bridge rectifier showing the input and output waveforms.

**Question 4**

There are four possible connection configurations a 3 phase transformer banks – the Y – Y, Y –  $\Delta$ ,  $\Delta$  –  $\Delta$  and  $\Delta$  – Y configurations. Draw the wiring of each of these configurations indicating the in each case, the relationship between the primary voltage and the secondary voltage.

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Subject: ELE303 - Fundamentals of Electrical Engineering

Time Allowed: 2 hours

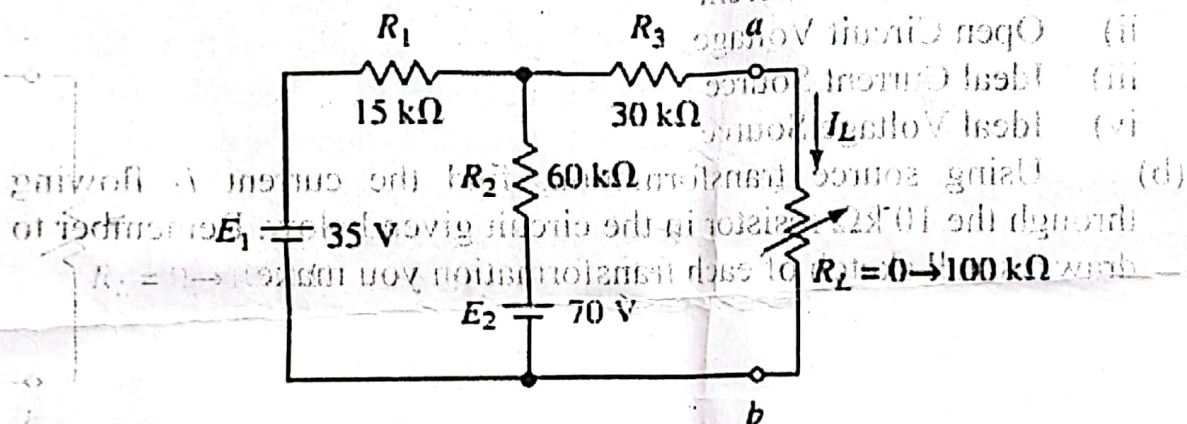
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Answer all 3 questions. You are reminded of the necessity for orderly presentation of your answers. Documents are NOT allowed. Start answering each question on a new page.

Note: All questions carry equal marks

**Question 1**

Consider the circuit below:



(a) Find the Norton (equivalent external to  $R_L$  in the circuit (looking between the points  $a$  and  $b$ ).

(b) Solve for the current  $I_L$  when  $R_L = 0, 10\text{ k}\Omega, 50\text{ k}\Omega$ , and  $100\text{ k}\Omega$

(c) What is the value of  $R_L$  for which maximum power is delivered to it from the circuit?

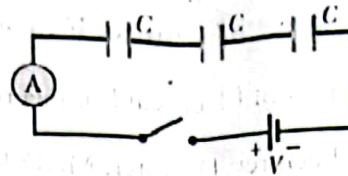
**Question 2**

(a) The figure below shows an open switch, a battery of potential difference  $V$ , a current-measuring meter  $A$ , and three identical uncharged capacitors of capacitance  $C$ . When the switch is closed and the circuit reaches equilibrium, what are?

(i) the potential difference across each capacitor and



- (ii) the charge on the left-hand plate of each capacitor?  
Give your answers in terms of  $C$  and  $V$ .



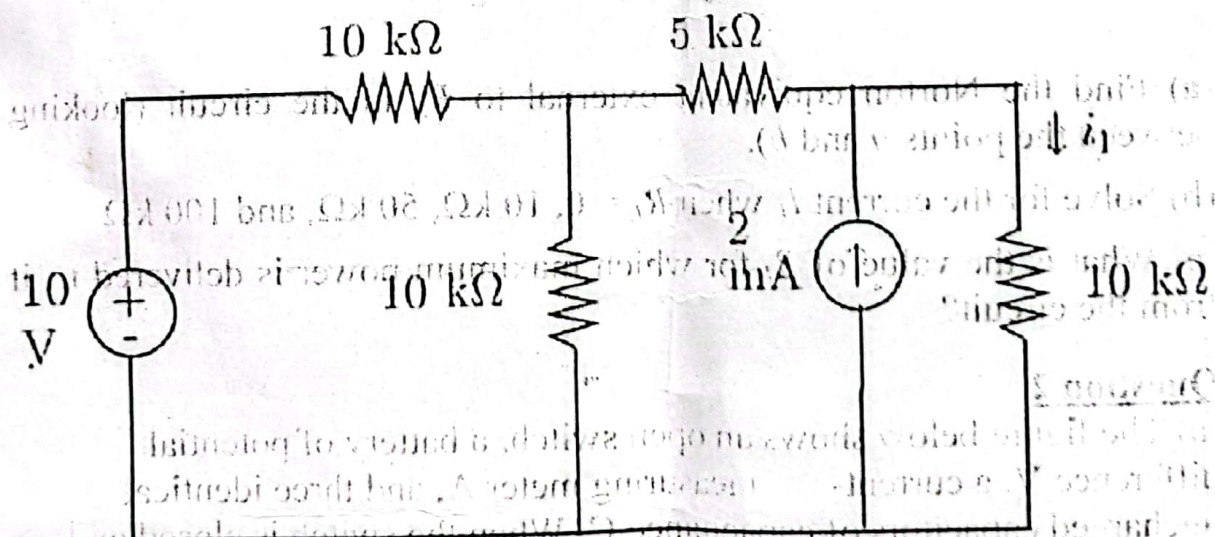
- (b) Most homes use solid copper wire having a diameter of 1.63 mm to provide electrical distribution to outlets and light sockets. Determine the resistance of 75 meters of a solid copper wire having the above diameter. Take the resistivity of copper to be  $1.723 \times 10^{-8} \Omega \cdot \text{m}$ .

### Question 3

(a) Explain the following:

- i) Short Circuit Current
- ii) Open Circuit Voltage
- iii) Ideal Current Source
- iv) Ideal Voltage Source

(b) Using source transformation, find the current  $i_1$  flowing through the  $10 \text{ k}\Omega$  resistor in the circuit given below. Remember to draw a small sketch of each transformation you make.

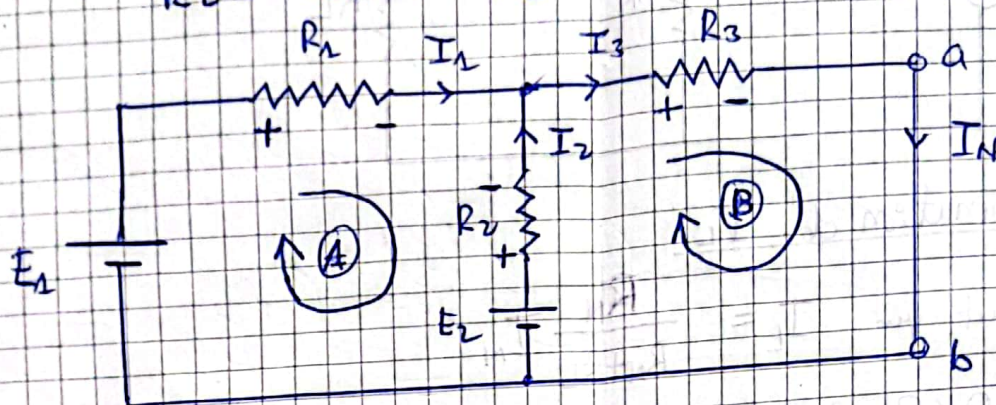




### Question 1

a) Déterminons le circuit équivalent de Norton

Données:  $R_1 = 15\text{ k}\Omega$   $R_3 = 30\text{ k}\Omega$   $E_1 = 35\text{ V}$   
 $R_2 = 60\text{ k}\Omega$   $R_L = 0 \rightarrow \infty\text{ k}\Omega$   $E_2 = 70\text{ V}$



KCL:  $I_3 = I_1 + I_2$  (1)

KVL  
 maille (A)  $-E_1 - R_1 I_1 + R_2 I_2 + E_2 = 0 \Rightarrow -35 - 15I_1 + 60I_2 + 70 = 0$   
 maille (B)  $-E_2 - R_2 I_2 - R_3 I_3 = 0 \Rightarrow -70 - 60I_2 - 30I_3 = 0$

$$\Rightarrow \begin{cases} -15I_1 + 60I_2 = -35 \\ 60I_2 + 30I_3 = -70 \end{cases} \Rightarrow \begin{cases} -3I_1 + 12I_2 = -7 & (2) \\ 6I_2 + 3I_3 = -7 & (3) \end{cases}$$

De (1), (2) et (3) on obtient:

$$\begin{cases} I_3 = I_1 + I_2 \\ -3I_1 + 12I_2 = -7 \\ 6I_2 + 3I_3 = -7 \end{cases} \Rightarrow \begin{cases} I_3 = I_1 + I_2 \\ -3I_1 + 12I_2 = -7 \\ 6I_2 + 3(I_1 + I_2) = -7 \end{cases}$$

$$\Rightarrow \begin{cases} I_3 = I_1 + I_2 \\ -3I_1 + 12I_2 = -7 \\ 3I_1 + 9I_2 = -7 \end{cases} \Rightarrow 21I_2 = -14 \Rightarrow I_2 = -\frac{2}{3}$$

$$3I_1 + 9I_2 = -7 \Rightarrow I_1 = \frac{1}{3}(-7 - 9I_2) = -\frac{1}{3}$$

$$I_3 = -\frac{1}{3} - \frac{2}{3} = -1$$

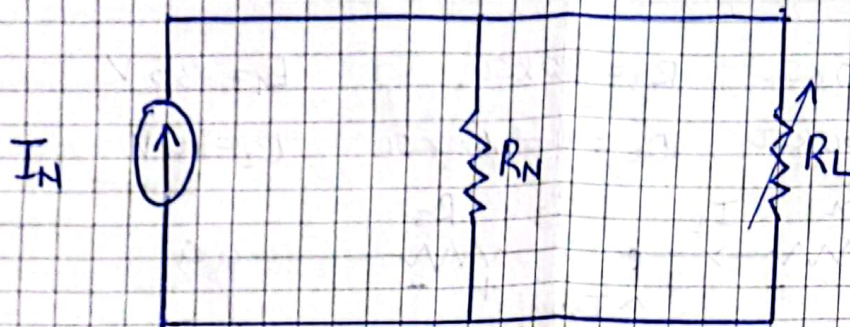
Ainsi  $I_1 = \frac{1}{3}\text{ mA}$ ,  $I_2 = -\frac{2}{3}\text{ mA}$  et  $I_3 = 1\text{ mA}$

De cela on trouve  $I_N = I_3 \Rightarrow \boxed{I_N = 1\text{ mA}}$



$$R_N = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}} + R_3 = \frac{R_1 R_2}{R_1 + R_2} + R_3 = \frac{15 \times 60}{15 + 60} + 30 = 42 \text{ k}\Omega$$

$$R_N = 42 \text{ k}\Omega$$



b) Détermination de  $I_L$

$$\text{On sait que } I_L = \frac{R_N}{R_N + R_L} I_N$$

$$\text{Pour } R_L = 0 \text{ k}\Omega \Rightarrow I_L = 1 \text{ mA}$$

$$\text{Pour } R_L = 10 \text{ k}\Omega \Rightarrow I_L = \frac{42}{42 + 10} \times 1 = 0,81 \text{ mA}$$

$$\text{Pour } R_L = 50 \text{ k}\Omega \Rightarrow I_L = \frac{42}{42 + 50} \times 1 = 0,457 \text{ mA}$$

$$\text{Pour } R_L = 100 \text{ k}\Omega \Rightarrow I_L = \frac{42}{42 + 100} \times 1 = 0,3 \text{ mA}$$

c) Valeur de  $R_L$  pour lequel on a une puissance maximale

$$\text{On sait que } P = R_L \cdot I_L^2 = R_L \left( \frac{R_N}{R_N + R_L} I_N \right)^2 = R_N^2 I_N^2 \cdot \frac{R_L}{(R_N + R_L)^2}$$

$$P = P_{\max} \Rightarrow \frac{dP}{dR_L} = 0$$

$$\frac{dP}{dR_L} = \frac{d \left( R_N^2 I_N^2 \cdot \frac{R_L}{(R_N + R_L)^2} \right)}{dR_L} = R_N^2 I_N^2 \cdot \frac{(R_N + R_L)^2 - 2R_L(R_N + R_L)}{(R_N + R_L)^4}$$

$$= R_N^2 I_N^2 \cdot \frac{R_N + R_L - 2R_L}{(R_N + R_L)^3} = \frac{R_N - R_L}{(R_N + R_L)^3}$$

$$\frac{dP}{dR_L} = 0 \Rightarrow R_N - R_L = 0$$

$$\text{Soit } R_N = R_L \Rightarrow R_L = 42 \text{ k}\Omega$$



### Question 3

a) Expliquons les termes suivants:

#### i) Courant de Court-Circuit

Le courant de Court-Circuit (ou intensité de Court-Circuit) noté  $I_{cc}$  d'un dipôle est le courant qui le traverserait si ses bornes étaient reliées par un conducteur parfait de résistance nulle.

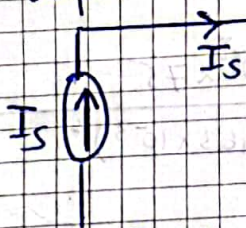
Pour le cas d'un dipôle linéaire, le courant de Court-Circuit permet de déterminer le courant de Norton utile pour établir le modèle équivalent de Norton d'un dipôle actif linéaire.

#### ii) Tension en Circuit ouvert

La tension de circuit ouvert, notée  $U_{co}$  également dite tension en circuit ouvert, est la tension électrique entre les bornes d'un appareil déconnecté de tout circuit.

#### iii) Source idéale de courant

Une source de courant idéale fournit un courant constant indépendamment de la tension apparaissant à ses bornes. La tension dépend de la résistance de charge  $R$  ( $V = RI$ ).

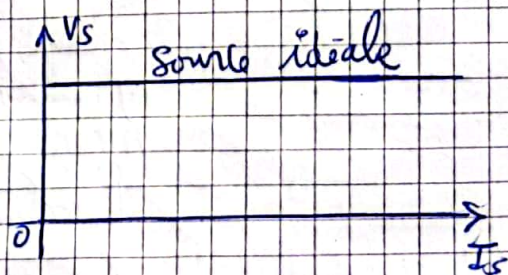
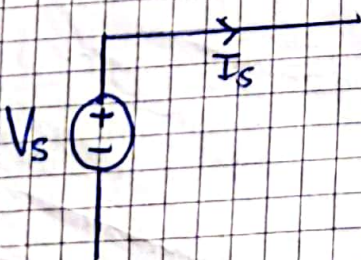


Source de courant idéale.



#### iv) Source de tension idéale

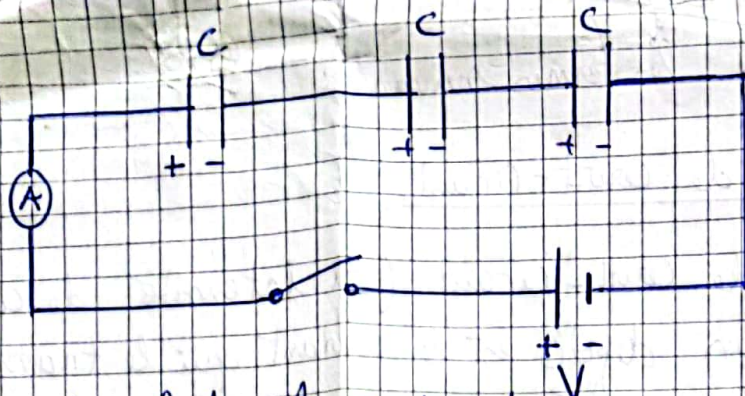
Une source de tension idéale fournit une tension  $V_0$  constante entre les bornes, quel que soit le courant  $I$  débité.





1) Question 2

a)



i) Différence de potentiel dans les condensateurs

Montage en série  $\Rightarrow C_{eq} = \frac{1}{\frac{1}{C} + \frac{1}{C} + \frac{1}{C}} = \frac{C}{3}$

Or  $Q = C_{eq} \cdot V = C \cdot V_i \Rightarrow V_i = \frac{C_{eq} V}{C} = \frac{\frac{C}{3} V}{C} = \frac{V}{3}$

$$V_i = \frac{V}{3}$$

ii) Charge du côté gauche du condensateur.

La charge du côté gauche du condensateur est positive

$$q_{gauch} = C \cdot V_i = \frac{C V}{3}$$

b) Résistance R

Données:  $D = 1,63 \text{ mm}$ ,  $l = 75 \text{ m}$ ,  $\rho = 1,723 \times 10^{-8} \Omega \cdot \text{m}$ .

On sait que

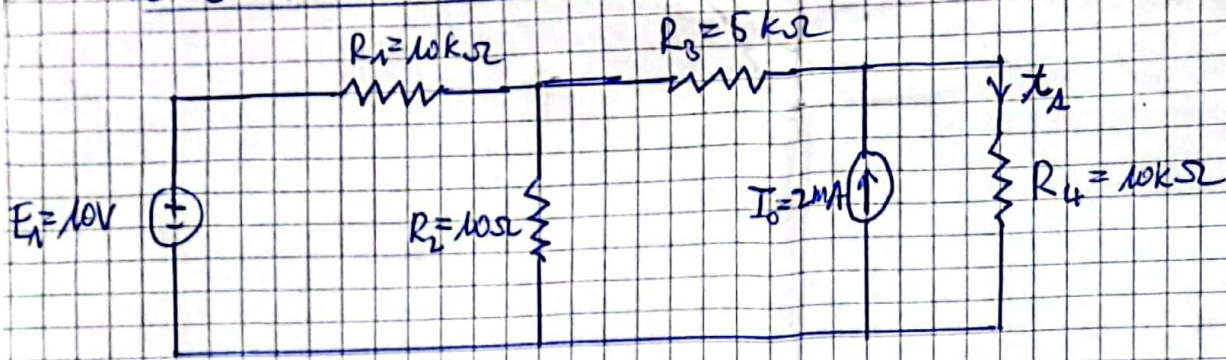
$$R = \frac{\rho l}{S} \quad \text{or} \quad S = \frac{\pi D^2}{4}$$

$$R = \frac{4 \rho l}{\pi D^2} = \frac{4 \times 1,723 \times 10^{-8} \times 75}{3,14 \times (1,63 \times 10^{-3})^2}$$

$$R = 0,619 \Omega$$

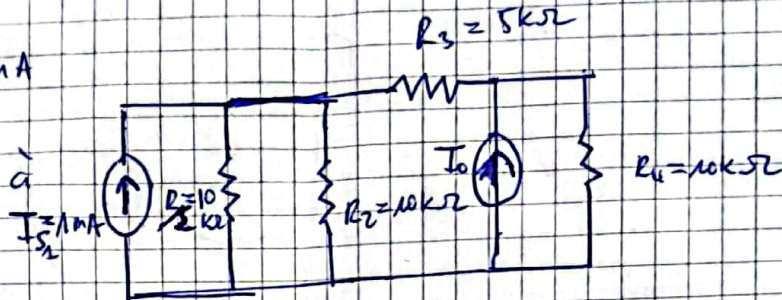


b) En utilisant les transformations de sources, déterminons le courant  $i_1$  traversant le résistor de résistance  $10\text{ k}\Omega$



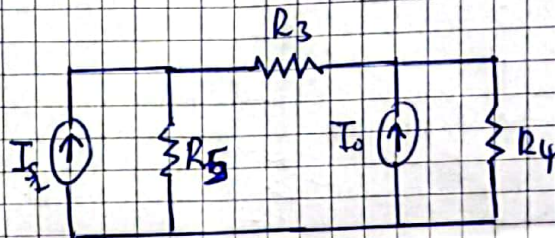
$$I_{S1} = \frac{E_1}{R_1} = \frac{10\text{ V}}{10\text{ k}\Omega} = 1\text{ mA}$$

Le circuit est équivalent à



$$R_5 = \frac{1}{\frac{1}{10} + \frac{1}{10}} = 5\text{ k}\Omega$$

Le circuit est équivalent à



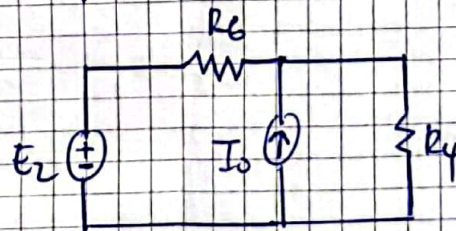
$$E_2 = I_{S1} R_5 = 5\text{ V}$$

Le circuit est équivalent à



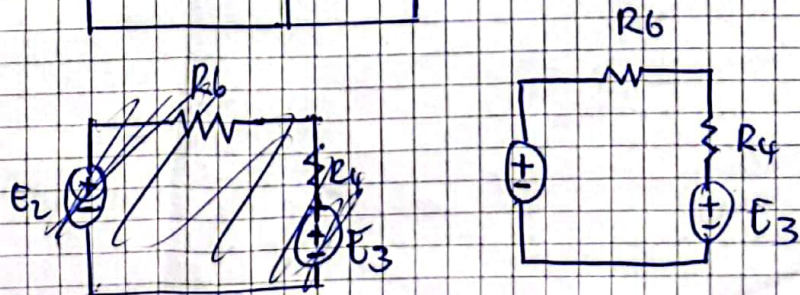
$$R_6 = R_5 + R_3 = 10\text{ k}\Omega$$

Le circuit équivalent à



$$E_3 = I_0 R_4 = 20\text{ V}$$

Le circuit équivalent à



KVL: 
$$i_1 = \frac{E_2 + E_3}{R_6 + R_4} = \frac{20 + 5}{10 + 10} = \frac{25}{20} = 1,25\text{ mA}$$

$$i_1 = 1,25\text{ mA}$$